

# Rectangular Divisor Cordial Graphs

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**Abstract**—In this paper, we introduce some rectangular divisor cordial graphs. Further, we can prove that the graphs obtained by the identification of some vertices of a divisor cordial graphs to certain notebook graphs are divisor cordial.

**Index Terms**—Divisor Cordial graph, Vertices, edges, notebook.

## I. INTRODUCTION

Number Theory is a fascinating subject in mathematics. It has so many interesting concepts. The concepts of primality and divisibility play an important role in Number Theory [1].

### Definition-1:

Let  $G = (V, E)$  be the function of  $f: v$  is denoted by the set  $\{0, 1\}$  with an each edge  $xy$ , is ascribed by the label 1 if  $f(x)$  divides  $f(y)$  or  $f(y)$  divides  $f(x)$  and 0 otherwise, then the number of edges labeled with 0 and the number of edges labeled with 1 differ by at most 1.

For each edge  $xy$ , assign the label 1 if either  $[f(x)]^2 | f(y)$  or  $[f(y)]^2 | f(x)$  and the label 0 otherwise.  $f$  is called a rectangular divisor cordial labeling if  $|e_f(0) - e_f(1)| \leq 1$ . A graph with a rectangle square divisor cordial labeling is called a rectangular divisor cordial graph.

### Definition-1.1

One edge union of cycles having same length is called a notebook. By common, the edge is said to be the base of the notebook. If we assume  $t$  copies of cycles of length  $m$  then the notebook is denoted by  $N_m^{(t)}$ . Note that  $N_m^{(t)}$  has  $(m-2)t + 2$  vertices and  $(m-1) + 1$  edges.

## II. MATHEMATICAL FORMULATION

### Theorem: 2.1

A notebook  $N$  with rectangular pages is divisor cordial.

### Proof:

Let  $N$  be the notebook with rectangular pages. Note that it has  $2t + 2$  vertices and  $3t + 1$  edges. Label the vertices of common edge by 1 and 2. Then label the vertices of the edges which are parallel to common edge as given below.

### Example: 2.2

Let us consider the notebook  $N$  with 2 rectangular pages. Note that it has 6 vertices and 7 edges. Here, we have  $e_f(0) = 3$  and

$$e_f(1) = 4.$$

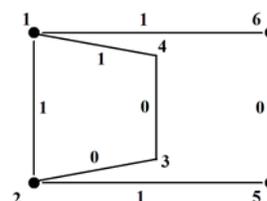


Fig. 1. Notebook has 2 rectangular pages

In the first page, label the numbers 4 and 3, second page 5 and 6,. Since 1 divides all the integers it contributes  $t+1$  to  $e_f(1)$ , 2 divides all the even integers it contributes  $\frac{t}{2}$  to each  $e_f(0)$  and  $e_f(1)$ .

When  $t$  is even,

$$e_f(0) = \frac{t+1}{2} \text{ and } e_f(1) = \frac{t-1}{2}.$$

When  $t$  is odd,  $m \neq m+1$  for any integer  $m > 1$ , the parallel edges are assigned  $t$  to  $e_f(0)$ .

Consequently,

Case (1) if  $t$  is even,

$$e_f(0) = \frac{3t}{2} \text{ and } e_f(1) = \frac{3t}{2} + 1 \text{ and}$$

Case (2) if  $t$  is odd, then

$$e_f(0) = \frac{3t+1}{2} \text{ and } e_f(1) = \frac{3t+1}{2}$$

Thus,  $|e_f(0) - e_f(1)| \leq 1$ . As a consequence,  $N$  shows divisor cordial.

### Corollary:2.3

A notebook with even number of rectangular pages is divisor dominated cordial but not strict.

### Proof:

The notebook  $N$  is divisor dominated cordial graph. If we interchange the labels of second page, then  $N$  becomes non divisor dominated cordial.

### Theorem: 2.4.

Let  $G$  be a divisor cordial graph and  $N$  be the notebook with rectangular pages. Then  $G_N^*$  is divisor cordial.



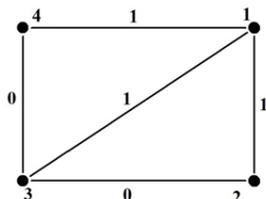


Fig. 6. Notebook divisor cordial graph G of even or odd size

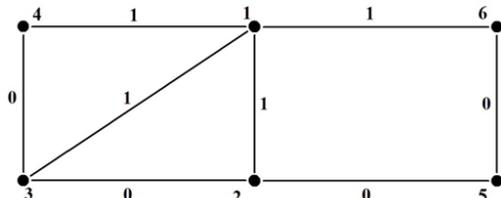


Fig. 7. Notebook with rectangular pages is adjacent

Here, we see that  $e_f(0) = 4$  and  $e_f(1) = 4$

### III. CONCLUSION

The notebook of the rectangular divisor cordial graphs is discussed and also, we can prove that the graphs obtained by the identification of some vertices of a divisor cordial graphs to certain notebook graphs are divisor cordial.

### REFERENCES

- [1] D. M. Burton, *Elementary Number Theory*, Second Edition, Wm. C. Brown Company Publishers, 1980.