Model Reference Adaptive Control of Overhead Crane

Liji Ramesan Santhi¹, V. Vishu²

¹Assistant Professor, Department of Electrical and Electronics Engineering, Vidya Academy of Science and Technology Technical Campus, Thiruvananthapuram, India
²JTO, BSNL, Thiruvananthapuram, India

Abstract: In the past decade's industrial cranes have been increasingly utilized as indispensable engineering equipment in various fields. The under actuated structure of the crane makes it hard to control. The achievement of both transporting trolley to target position and reducing payload swing is not always easy in real cases. Usually conventional feedback controllers may not perform well online because of the variation in process dynamics due to nonlinearities, changes in environmental conditions and variation in the character of the disturbances. To resolve the above said problem, this paper deals with the designing of a controller for an overhead crane with Model Reference Adaptive Control (MRAC) scheme using the MIT rule for adaptive mechanism. In this control scheme, a cost function is defined as a function of error between the outputs of the process and the reference model, and controller parameters are varied in such a way that the cost function is minimized.

Keywords: Crane, Model Reference Adaptive Control (MRAC), Under actuated structure.

1. Introduction

The main purpose of control of an overhead crane is to transport the load to the desired location with less swing. Most of the crane used in industry results in a swing movement when payload is suddenly stopped after a fast motion. The overhead crane are used in the factories mainly in hazardous areas like nuclear power plant due to its low cost, easy assembly, precise positioning of load and less maintenance. The swing motion can be decreased to some extent by adjusting the speed of the motor but it will be time-consuming process. A skillful operator is needed to control both the position and swing manually. The lack of efficiency in controlling the crane also might cause problems and create harm to the people and the surroundings.

Various methods were done on cranes system based on open loop control system. Earlier open loop time optimal strategies were applied to the crane system by many researchers such as discussed in [2], [3]. The results showed that open loop approach is sensitive to the system parameters and could not compensate for disturbances due to wind. Another importance of open loop method is the input shaping introduced by Karnopp [4], Teo [5] and Singhose [6]. However, the input shaping method is also again an open-loop approach. Hubbel et al. [7] used an open-loop method to control the movement of the crane. In this open loop control strategy, the input control profile was determined in such a way that unwanted oscillations and residual pendulations were neglected. However, their approach was applicable, but the open loop control technique is not robust to disturbances and parameter uncertainties [8]. Moreover, a feedback PID anti-swing controller is developed in [9] for controlling overhead crane. Ahmad et al. [10] used a hybrid input-shaping approach to control of the crane. Wahyudi and Jalani [11] introduced fuzzy logic feedback control technique to control the crane system. They also presented an optimal control technique is used in [12] to control the oscillatory motion of the crane. Here, minimum energy of the system and also integrated absolute error of the payload angle are considered as their optimization criterion. Zhao and Gao [13] studied the control of the overhead crane. They introduced a fuzzy control strategy to control the input delay and actuator saturation of the system. Nazemizadeh et al. [14] studied tracking control of the crane. Furthermore, Nazemizadeh [15] presented a PID tuning method for tracking control of a crane.

In this paper, overhead crane is provided with a IMC to control both swing and position of the crane and the results are compared with conventional PD and PID control. This paper is organized in the following order. The modeling of the crane is explained in section 2. Section 3 discusses about the crane with conventional PD and PID controller. Section 4 discusses about the crane with MRAC. Simulation results using different controllers is given in section 5. In section 6, the conclusion of this paper is discussed.

2. Modelling of crane

Figure 1 represents a schematic diagram of the crane considered in this paper. Due to the fact that only two-dimensional motion of crane is considered in this paper, there are two independent coordinates namely y and θ, to describe the trolley position and the swing angle of the payload respectively.

Since the mass of the rope used in the crane is small enough as compared to the payload mass, it is assumed to be massless. The non-linear dynamic model of overhead crane prototype is derived by using Lagrange equations.
(m_t + m_p)\ddot{y} = F_y + m_p l (\ddot{\theta}_y \sin \theta_y - \dot{\theta}_y \cos \theta_y) \quad (1)

\cos \theta_y \ddot{y} + l \dot{\theta}_y = -g \sin \theta_y \quad (2)

By assuming small value of \(\theta_y\), the following linearized model of the crane is found out.

(m_p + m_t)\ddot{y} + m_p l \dot{\theta}_y = F_y \quad (3)

\dot{y} + l \dot{\theta}_y + g \theta_y = 0 \quad (4)

In the equation given above, m is the mass of the trolley, m_p is mass of the payload, 1 is the length of the rope, y is the position of the trolley, \(\theta_y\) is the swing angle and Fy is the force supplied by the dc motor. Thus the state space model of the crane system can be obtained as

\[ X = Ax + Bu \]

\[ Y = Cx + Du \]

where

\[ A = \begin{bmatrix} 0 & 1 & 0 & m_p & \theta & 0 \\
0 & 0 & 0 & m_t & \theta & 0 \\
0 & 0 & 0 & (m_t + m_p) & \theta & 0 \\
0 & 0 & 0 & 0 & 1 & 0 \\
\end{bmatrix} \]

\[ B = \begin{bmatrix} \frac{1}{m_t} \\
0 \\
0 \\
-\frac{1}{m_t} \\
\end{bmatrix} \]

\[ C = \begin{bmatrix} 1 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 \\
\end{bmatrix} \quad D = [0] \]

\[ X = [y \quad \dot{y} \quad \theta_y \quad \dot{\theta}_y]^T \]

The translational motion of the trolley is supplied by DC motor. Therefore, to find out the entire model of the crane, the motor dynamic is modeled according to equivalent DC motor circuit. The equivalent circuit of DC motor has an armature voltage to the dc motor \(V\), armature current I and damping constant B. The rotational motion is transformed to translational motion through the mechanical part (pulley or gear) with radii of r. The dynamics of dc motor circuit is given below by the following equations,

\[ V = RI + \frac{1}{R} \frac{dl}{dt} + k_b \theta \]

\[ T = k_t I \]

\[ J(\ddot{\theta}) + B(\dot{\theta}) = T \]

Table 1

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>m_p</td>
<td>0.23</td>
<td>Kg</td>
</tr>
<tr>
<td>m_t</td>
<td>1.073</td>
<td>Kg</td>
</tr>
<tr>
<td>L</td>
<td>0.3302</td>
<td>m</td>
</tr>
<tr>
<td>G</td>
<td>9.81</td>
<td>m/s^2</td>
</tr>
<tr>
<td>R</td>
<td>0.006</td>
<td>m</td>
</tr>
<tr>
<td>R</td>
<td>2.6</td>
<td>\Omega</td>
</tr>
<tr>
<td>L</td>
<td>2.5 \times 10^{-3}</td>
<td>H</td>
</tr>
<tr>
<td>J</td>
<td>2 \times 10^{-5}</td>
<td>Kg/m^2</td>
</tr>
<tr>
<td>B</td>
<td>5 \times 10^{-4}</td>
<td>Nms/rad</td>
</tr>
<tr>
<td>k_p</td>
<td>0.00767</td>
<td>Nm/A</td>
</tr>
<tr>
<td>k_t</td>
<td>0.00767</td>
<td>V/srad</td>
</tr>
</tbody>
</table>

Table 2

| Optimised PID and PD position and anti-swing gains |
|--------|--------|--------|--------|
| K_p    | K_i    | K_d    | K_ds   |
| 140.4  | 0.7    | 136.5  | 43.5   |

3. Crane control with PID and PD controller

The conventional PID and PD controllers are used to analyse the ability of the proposed model-based soft sensor. The function of the controller is to control the payload position \(Y(s)\) so that it moves to the desired position \(Y(t)\) as fast as possible without larger swing angle \(\theta_y\). A PID controller is used in the system to control the position of the crane, while a PD controller is used for controlling the swing angle. The values of the controller gains used in PID and PD controllers are designed and optimized with simulation model by using Simulink library block. The PID controller is optimized. Moreover, in order to reduce the value of the swing angle quickly, the PD controller is optimized. Thus there are five parameters to be optimized in order to have satisfactory control performance. The parameters, \(K_p\), \(K_i\), \(K_d\), \(K_{p_s}\) and \(K_{d_s}\) which are the proportional, integral and derivative gains for the position control and proportional, derivative gains for the anti-swing control. The optimization to obtain PID and PD controller gains for position and anti-swing crane control was done by using Ziegler Nichols tuning method. Based on the result, the gains of \(K_p\), \(K_i\), \(K_d\), \(K_{p_s}\) and \(K_{d_s}\) are shown in Table 2.

4. Model reference adaptive controller (MRAC)

In the adaptive control scheme, the controller parameters are varied (in an automatic fashion) to sync with the changes in the process characteristics. It is known that if properly designed, this procedure will be a significant improvement over the classical scheme.

Adaptive control methods are of various types, differing mainly in the way the controller parameters are varied.
Scheduled adaptive control, model reference adaptive control, and self-tuning controllers are considered the most popular control methods.

The prime component of the Model Reference Adaptive Controller (MRAC) scheme is the reference model. This reference model consists of a reasonable closed-loop model which defines how the process should be responded to a set-point change. This could be as simple as a reference trajectory, or it could be more detailed closed-loop model. The outputs of the reference model and actual process are compared and the noted error $e_m$ is utilised to drive some adaptation scheme to adjust the controller parameters so as to reduce $e_m$ to zero. The adoption scheme could be some control parameter optimization algorithm that decreases the integral squared value of $e_m$ or some other procedure. This is an adaptive control method where the performance specifications are given in terms of a model. The model represents the ideal response of the process to a given command signal. The controller has two loops. The inner loop, which is an ordinary feedback loop which consists of the process and the controller. The outer loop, which adjust the controller parameters in such a way that the error $e = y - y_m$ should be small (not trivial).

![Model reference adaptive controller](image)

**Tracking error:**  
$e = y - y_m$

Introduce the cost function $J$:

$$J(\theta) = \frac{1}{2} e^2$$

where $\theta$ is a vector of controller parameters. Here the parameters are changed in the direction of the negative gradient of $e^2$.

$$\frac{d\theta}{dt} = -\gamma \frac{\partial J}{\partial \theta} = -\gamma e \frac{\partial e}{\partial \theta}$$

MIT Rule

$\frac{\partial e}{\partial \theta}$ is called the sensitivity derivative. This derivative indicates how the error is influenced by the adjustable parameters $\theta$.

The loss function can also be chosen as

$$J(\theta) = \|e\|

$$d\theta/dt = -\gamma \frac{\partial e}{\partial \theta} \text{ sign } e$$

First MRAC is implemented by this function

$$d\theta/dt = -\gamma \text{ sign } \frac{\partial e}{\partial \theta} \text{ sign } (e) \text{ [sign-sign algorithm]}$$

It is used in telecommunication where simple implementation and fast computing are required.

### 5. Simulation results

MATLAB software package is used in the crane system to determine the response of the system. The Simulink model of the system with the optimized values of PD and PID controller gains is created in MATLAB. The Simulink model of the system is developed. The figure 4 shows the position and swing angle control using optimized values for PD and PID controller. From figure 5 and figure 6, the system is regulated at 5 sec and 2 sec respectively and the system consists of small number of overshoot and undershoot when compared to PD and PID controller. The system is precisely regulated at this condition. MRAC control the position and swing without undershoot in spite of the disturbances.

![Position control using MRAC](image)

**Fig. 4. Position control using MRAC**

![Swing angle control using MRAC](image)

**Fig. 5. Swing angle control using MRAC**

### 6. Conclusion

A detailed discussion on MRAC scheme using MIT rule is
done in this paper and the performance evaluation is carried out by means of simulations on SIMULINK. This paper compares the model reference adaptive control with conventional PD and PID controller. MRAC is less sensitive even to large amplitude disturbances.

References